

Factor Analysis and Measurement Invariance. Workshop 2.

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Definition

Measurement invariance tests for the **psychometric equivalence of a construct across different target cultures** (Greiff & Iliescu, 2017). Cross-cultural comparability is usually evaluated through multigroup confirmatory factor analysis (MGCFA), which is a technique capable of testing cross-national equivalence over several countries (Jöreskog, 1971; Meitinger, 2017) to claim that a construct is fully invariant.

How can you test M.I.?

Measurement invariance can be tested across four steps: **Configural**, **Metric**, **Scalar**, and **Strict** (see Putnick & Bornstein, 2016), following the recommendations by Hu and Bentler (1999), Cheung and Rensvold (2002), Chen (2007), and Meade et al. (2008). Either ML or MLR estimator are the usual choice (Maximum likelihood, and ML with robust standard errors) across tested steps. Applied decision rules to whether they complied or not with the type of studied invariance should be based on sample size, type of invariance, and fit-statistic used for comparison (see Meade et al., 2008).

Types of invariance to be tested

The nested models are progressively tested from configural to scalar invariance (Vandenberg & Lance, 2000). **Configural invariance** represents the baseline, which assumes that groups share the same conceptual framework without equality constraints on any parameter. **Metric invariance** requires equivalence of factor loadings, meaning that each item contributes to the latent construct similarly across different groups.

Types of invariance to be tested

Scalar invariance allows for the comparison of latent means across groups (Putnick & Bornstein, 2016). This type of invariance analysis derives from constraining intercepts to be equal among groups. If there is enough evidence for scalar invariance, then scores are considered invariant, i.e., equivalent (Chen, 2007; Tóth-Király et al., 2017). The previous types of invariance are necessary to claim that a construct is fully invariant. In **Strict invariance**, residuals are set to be equal across groups, although this is optional in cross-cultural research.

Some examples from PYD research

Marique-Millones et al., 2021

Table 2 Invariance models for the 7Cs and risky behaviors

	Model fit		
	χ^2 (df)	RMSEA	CFI
The 7Cs model			
Competence	52.45 (13)	.063	.965
Confidence	132.28 (27)	.072	.965
Character	153.31 (45)	.057	.937
Caring	52.90 (19)	.049	.983
Connection	152.48 (43)	.058	.944
Contribution	64.78 (14)	.069	.915
Creativity	177.01 (56)	.054	.969
Risky behaviors	7.51 (5)	.026	.963

Note. χ^2 = Chi-Square tests significant at $p < .01$; df = degrees of freedom; CFI = Comparative Fit Index; RMSEA = Root Mean Square Error of Approximation. The represented models for each construct refer to the measurement weights model indicating construct invariance across samples

Uka et al., 2021

Table 3 Measurement invariance for the developmental assets across countries

Model	Model fit indices			
	S-B χ^2 (df)	RMSEA	90% CIs RMSEA	CFI
Configural invariance	150.093 (76)	.071	.054–.087	.952
Metric invariance	170.356 (94)	.065	.049–.080	.951
Scalar invariance	242.115 (112)	.077	.064–.091	.917
Partial scalar invariance	204.404 (107)	.068	.054–.082	.937

Note. S-B χ^2 = Satorra-Bentler scaled χ^2 ; df = degrees of freedom; CIs = Confidence Intervals; RMSEA = Robust Root Mean Square Error of Approximation; CFI = Comparative Fit Index. Configural invariance tests whether all items/factors are associated with the assets allowing for subsequent tests to be conducted. Metric invariance tests whether all items/factors are associated with assets in the same way allowing the comparison of relations between these factors and other constructs. Scalar/partial invariance constrains factor loadings and intercepts to be equal among groups allowing to compare mean differences of the measured factors

Kosic et al., 2021

Table 2 Fit statistics for multi-group confirmatory factor analyses for measures used with Slovene and Italian youth

	Model fit			
	χ^2	df	CFI	RMSEA
Measure				
Social support				
Configural invariance	75.44***	24	.909	.064
Metric invariance	78.69***	30	.914	.052
Scalar invariance	159.14***	37	.785	.072
Social competence				
Configural invariance	41.18***	22	.949	.041
Metric invariance	50.66***	28	.939	.039
Scalar invariance	58.72***	35	.936	.036
Positive identity				
Configural invariance	7.91	4	.995	.043
Metric invariance	9.40	7	.997	.026
Scalar invariance	15.45	11	.994	.028
Model test				
Unconstrained model	16.32***	4	.928	.077
Structural weights model	19.34***	7	.928	.058
Structural residuals model	21.62	12	.944	.039

Some examples from PYD research

Mplus VERSION 8.3
MUTHEN & MUTHEN
04/20/2022 5:42 PM

INPUT INSTRUCTIONS

TITLE: Multiple Group Configural Invariance Gender Confi. Metric and Scalar.

DATA:

FILE IS "C:\Dataset_PYD_Spain_and_Chile_For_MI.dat";
VARIABLE:
names= Gender Age Country d1 d2 d3 d4 d5 d6 d7 d8
d9 d10 d11 d12 d13 d14 d15 d16 d17 d18 d19 d20 d21
d22 d23 d24 d25 d26 d27 d28 d29 d30 d31 d32 d33 d34;

grouping is Gender (1=Woman 2=Man);

ANALYSIS:

ESTIMATOR = MLR;
ROTATION = TARGET (orthogonal);
MODEL = CONFIGURAL METRIC SCALAR;

OUTPUT:

sampstat;

MODEL:

fg BY d1-d34 (*1);

FS1 BY d1 d2 d3 d7 d8 d9 d4~0 d5~0 d6~0
d10~0 d11~0 d12~0 d13~0 d14~0 d15~0 d16~0
d17~0 d18~0 d19~0 d20~0 d21~0 d22~0 d23~0
d24~0 d25~0 d26~0 d27~0 d28~0 d29~0 d30~0
d31~0 d32~0 d33~0 d34~0(*1);

FS2 BY d4 d6 d10 d12 d13 d14 d1~0 d2~0 d3~0
d7~0 d8~0 d9~0 d5~0 d11~0 d15~0 d16~0 d17~0
d18~0 d19~0 d20~0 d21~0 d22~0 d23~0 d24~0
d25~0 d26~0 d27~0 d28~0 d29~0 d30~0 d31~0
d32~0 d33~0 d34~0(*1);

FS3 BY d5 d11 d15 d16 d17 d18 d19 d20
d1~0 d2~0 d3~0 d7~0 d8~0 d9~0 d4~0 d6~0
d10~0 d12~0 d13~0 d14~0 d21~0 d22~0 d23~0
d24~0 d25~0 d26~0 d27~0 d28~0 d29~0 d30~0
d31~0 d32~0 d33~0 d34~0(*1);

FS4 BY d21 d22 d23 d24 d25 d26 d1~0 d2~0
d3~0 d7~0 d8~0 d9~0 d4~0 d6~0 d10~0 d12~0
d13~0 d14~0 d5~0 d11~0 d15~0 d16~0 d17~0
d18~0 d19~0 d20~0 d27~0 d28~0 d29~0 d30~0
d31~0 d32~0 d33~0 d34~0(*1);

FS5 BY d27 d28 d29 d30 d31 d32 d33 d34
d1~0 d2~0 d3~0 d7~0 d8~0 d9~0 d4~0 d6~0
d10~0 d12~0 d13~0 d14~0 d5~0 d11~0 d15~0
d16~0 d17~0 d18~0 d19~0 d20~0 d21~0 d22~0
d23~0 d24~0 d25~0 d26~0(*1);

Global PYD

Competence

Confidence

Character

Caring

Connection

Mplus VERSION 8.3
MUTHEN & MUTHEN
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INPUT INSTRUCTIONS

TITLE: Multiple Group Configural Invariance Country Confi. Metric and Scalar.

DATA:

FILE IS "C:\Dataset_PYD_Spain_and_Chile_For_MI.dat";
VARIABLE:
names= Gender Age Country d1 d2 d3 d4 d5 d6 d7 d8
d9 d10 d11 d12 d13 d14 d15 d16 d17 d18 d19 d20 d21
d22 d23 d24 d25 d26 d27 d28 d29 d30 d31 d32 d33 d34;

grouping is Country (1=Spain 2=Chile);

ANALYSIS:

ESTIMATOR = MLR;
ROTATION = TARGET (orthogonal);
MODEL = CONFIGURAL METRIC SCALAR;

OUTPUT:

sampstat;

MODEL:

fg BY d1-d34 (*1);

FS1 BY d1 d2 d3 d7 d8 d9 d4~0 d5~0 d6~0
d10~0 d11~0 d12~0 d13~0 d14~0 d15~0 d16~0
d17~0 d18~0 d19~0 d20~0 d21~0 d22~0 d23~0
d24~0 d25~0 d26~0 d27~0 d28~0 d29~0 d30~0
d31~0 d32~0 d33~0 d34~0(*1);

FS2 BY d4 d6 d10 d12 d13 d14 d1~0 d2~0 d3~0
d7~0 d8~0 d9~0 d5~0 d11~0 d15~0 d16~0 d17~0
d18~0 d19~0 d20~0 d21~0 d22~0 d23~0 d24~0
d25~0 d26~0 d27~0 d28~0 d29~0 d30~0 d31~0
d32~0 d33~0 d34~0(*1);

FS3 BY d5 d11 d15 d16 d17 d18 d19 d20
d1~0 d2~0 d3~0 d7~0 d8~0 d9~0 d4~0 d6~0
d10~0 d12~0 d13~0 d14~0 d21~0 d22~0 d23~0
d24~0 d25~0 d26~0 d27~0 d28~0 d29~0 d30~0
d31~0 d32~0 d33~0 d34~0(*1);

FS4 BY d21 d22 d23 d24 d25 d26 d1~0 d2~0
d3~0 d7~0 d8~0 d9~0 d4~0 d6~0 d10~0 d12~0
d13~0 d14~0 d5~0 d11~0 d15~0 d16~0 d17~0
d18~0 d19~0 d20~0 d27~0 d28~0 d29~0 d30~0
d31~0 d32~0 d33~0 d34~0(*1);

FS5 BY d27 d28 d29 d30 d31 d32 d33 d34
d1~0 d2~0 d3~0 d7~0 d8~0 d9~0 d4~0 d6~0
d10~0 d12~0 d13~0 d14~0 d5~0 d11~0 d15~0
d16~0 d17~0 d18~0 d19~0 d20~0 d21~0 d22~0
d23~0 d24~0 d25~0 d26~0(*1);

Some examples from PYD research

Multiple Group Configural Invariance Country Confi, Metric and Scalar.

SUMMARY OF ANALYSIS

Number of groups	2
Number of observations	
Group SPAIN	899
Group CHILE	261
Total sample size	1160

Number of dependent variables	36
Number of independent variables	0
Number of continuous latent variables	6

Observed dependent variables

Continuous

GENDER	AGE	D1	D2	D3	D4
D5	D6	D7	D8	D9	D10
D11	D12	D13	D14	D15	D16
D17	D18	D19	D20	D21	D22
D23	D24	D25	D26	D27	D28
D29	D30	D31	D32	D33	D34

Continuous latent variables

EFA factors

*1: FG	FS1	FS2	FS3	FS4	FS5
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Variables with special functions

Grouping variable	COUNTRY
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Estimator	MLR
Rotation	TARGET
Row standardization	Varies
Type of rotation	ORTHOGONAL
Information matrix	OBSERVED
Maximum number of iterations	1000
Convergence criterion	0.500D-04
Maximum number of steepest descent iterations	20
Optimization Specifications for the Exploratory Factor Analysis	
Rotation Algorithm	
Number of random starts	30
Maximum number of iterations	1000000
Derivative convergence criterion	0.100D-04

Input data file(s)
C:\Dataset_PYD_Spain_and_Chile_For_MI.dat

Input data format FREE

Some examples from PYD research

MODEL FIT INFORMATION

Invariance Testing

Model	Number of Parameters	Chi-Square	Degrees of Freedom	P-Value
Configural	N/A**			
Metric	N/A**			
Scalar	N/A**			

** Model did not terminate normally. Refer to TECH9 output for more information.

MODEL RESULTS FOR THE CONFIGURAL MODEL

Estimate

Measurement Invariance by Country

TECHNICAL 9 OUTPUT

Error messages for the Configural Model:

THE MODEL ESTIMATION TERMINATED NORMALLY

WARNING: THE RESIDUAL COVARIANCE MATRIX (THETA) IN GROUP MAN IS NOT POSITIVE DEFINITE. THIS COULD INDICATE A NEGATIVE VARIANCE/RESIDUAL VARIANCE FOR AN OBSERVED VARIABLE, A CORRELATION GREATER OR EQUAL TO ONE BETWEEN TWO OBSERVED VARIABLES, OR A LINEAR DEPENDENCY AMONG MORE THAN TWO OBSERVED VARIABLES. CHECK THE RESULTS SECTION FOR MORE INFORMATION. PROBLEM INVOLVING VARIABLE D33.

Error messages for the Metric Model:

THE MODEL ESTIMATION TERMINATED NORMALLY

WARNING: THE RESIDUAL COVARIANCE MATRIX (THETA) IN GROUP WOMAN IS NOT POSITIVE DEFINITE. THIS COULD INDICATE A NEGATIVE VARIANCE/RESIDUAL VARIANCE FOR AN OBSERVED VARIABLE, A CORRELATION GREATER OR EQUAL TO ONE BETWEEN TWO OBSERVED VARIABLES, OR A LINEAR DEPENDENCY AMONG MORE THAN TWO OBSERVED VARIABLES. CHECK THE RESULTS SECTION FOR MORE INFORMATION. PROBLEM INVOLVING VARIABLE D33.

Error messages for the Scalar Model:

THE MODEL ESTIMATION TERMINATED NORMALLY

WARNING: THE RESIDUAL COVARIANCE MATRIX (THETA) IN GROUP WOMAN IS NOT POSITIVE DEFINITE. THIS COULD INDICATE A NEGATIVE VARIANCE/RESIDUAL VARIANCE FOR AN OBSERVED VARIABLE, A CORRELATION GREATER OR EQUAL TO ONE BETWEEN TWO OBSERVED VARIABLES, OR A LINEAR DEPENDENCY AMONG MORE THAN TWO OBSERVED VARIABLES. CHECK THE RESULTS SECTION FOR MORE INFORMATION. PROBLEM INVOLVING VARIABLE D33.

Measurement Invariance by Gender

Number of Free Parameters 354

Loglikelihood

H0 Value -52019.259
 H0 Scaling Correction Factor 1.3752
 for MLR
 H1 Value -50174.517
 H1 Scaling Correction Factor 1.2491
 for MLR

Information Criteria

Akaike (AIC) 104746.518
 Bayesian (BIC) 106536.404
 Sample-Size Adjusted BIC 105411.982
 (n* = (n + 2) / 24)

Chi-Square Test of Model Fit

Value 3057.801*
 Degrees of Freedom 1050
 P-Value 0.0000
 Scaling Correction Factor 1.2066
 for MLR

Chi-Square Contribution From Each Group

WOMAN 1887.207
 MAN 1170.594

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM a for chi-square difference testing in the regular way. chi-square difference testing is described on the Mplus and ULSMV difference testing is done using the DIFFTEST

RMSEA (Root Mean Square Error Of Approximation)

Estimate 0.057
 90 Percent C.I. 0.055 0.060
 Probability RMSEA <= .05 0.000

CFI/TLI

CFI 0.830
 TLI 0.796

Chi-Square Test of Model Fit for the Baseline Model

Value 13053.665
 Degrees of Freedom 1260
 P-Value 0.0000

SRMR (Standardized Root Mean Square Residual)

Value 0.059

Invariance Testing

Model	Number of Parameters	Chi-Square	Degrees of Freedom	P-Value
Configural	522	2827.895	882	0.0000
Metric	354	3057.801	1050	0.0000
Scalar	326	3123.549	1078	0.0000

Models Compared	Chi-Square	Degrees of Freedom	P-Value
Metric against Configural	275.407	168	0.0000
Scalar against Configural	335.168	196	0.0000
Scalar against Metric	63.684	28	0.0001

MODEL FIT INFORMATION FOR THE CONFIGURAL MODEL

Number of Free Parameters 522

Loglikelihood

H0 Value -51824.390
 H0 Scaling Correction Factor 1.3880
 for MLR
 H1 Value -50174.517
 H1 Scaling Correction Factor 1.2491
 for MLR

Information Criteria

Akaike (AIC) 104692.779
 Bayesian (BIC) 107332.103
 Sample-Size Adjusted BIC 105674.058
 (n* = (n + 2) / 24)

Chi-Square Test of Model Fit

Value 2827.895*
 Degrees of Freedom 882
 P-Value 0.0000
 Scaling Correction Factor 1.1669
 for MLR

CFI/TLI

CFI 0.835
 TLI 0.764

SRMR (Standardized Root Mean Square Residual)

Value 0.053

Chi-Square Contribution and P-Value From Each Group (degrees of freedom = 441)

WOMAN 1887.443 0.000
 MAN 940.452 0.000

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM and WLSMV cannot be used for chi-square difference testing in the regular way. MLM, MLR and WLSM chi-square difference testing is described on the Mplus website. MLMV, WLSMV, and ULSMV difference testing is done using the DIFFTEST option.

RMSEA (Root Mean Square Error Of Approximation)

Estimate 0.062
 90 Percent C.I. 0.059 0.064
 Probability RMSEA <= .05 0.000

MODEL FIT INFORMATION FOR THE SCALAR MODEL

Number of Free Parameters 326

Loglikelihood

H0 Value -52053.135
 H0 Scaling Correction Factor 1.4019
 for MLR
 H1 Value -50174.517
 H1 Scaling Correction Factor 1.2491
 for MLR

Information Criteria

Akaike (AIC) 104758.270
 Bayesian (BIC) 106406.583
 Sample-Size Adjusted BIC 105371.099
 (n* = (n + 2) / 24)

Chi-Square Test of Model Fit

Value 3123.549*
 Degrees of Freedom 1078
 P-Value 0.0000
 Scaling Correction Factor 1.2029
 for MLR

Chi-Square Contribution From Each Group

WOMAN 1904.460
 MAN 1219.089

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM and W for chi-square difference testing in the regular way. MLM chi-square difference testing is described on the Mplus web and ULSMV difference testing is done using the DIFFTEST of

RMSEA (Root Mean Square Error Of Approximation)

Estimate 0.057
 90 Percent C.I. 0.055 0.060
 Probability RMSEA <= .05 0.000

CFI/TLI

CFI 0.827
 TLI 0.797

Chi-Square Test of Model Fit for the Baseline Model

Value 13053.665
 Degrees of Freedom 1260
 P-Value 0.0000

SRMR (Standardized Root Mean Square Residual)

Value 0.060

Some examples from Trait EI research

TITLE: Multiple Group Omnibus Measurement Invariance.

DATA:

FILE IS "C:\full_new_dataset_clinical.dat";

VARIABLE:

names= education occupation civilstatus age gender

t1 t2 t3 t4 t5 t6 t7 t8 t9 t10 t11 t12 t13 t14 t15 t16 t17 t18 t19 t20 t21 t22 t23 t24 t25 t26 t27
t28 t29 t30;

usevar = t1 t2 t3 t4 t5 t6 t7 t8 t9 t10 t11 t12 t13 t14 t15 t16 t17 t18 t19 t20 t21 t22 t23 t24 t25
t26 t27 t28 t29 t30;

grouping is gender (1=Woman 2=Man);

ANALYSIS:

ESTIMATOR = MLR;

ROTATION = TARGET (orthogonal);

MODEL = CONFIGURAL METRIC SCALAR;

OUTPUT: sampstat;

MODEL:

fg BY t1-t30 (*1);

FS1 BY t5 t20 t9 t24 t12 t27 t4~0 t19~0
t7~0 t22~0 t15~0 t30~0 t1~0
t16~0 t2~0 t17~0 t8~0 t23~0 t13~0
t28~0 t6~0 t21~0 t10~0
t25~0 t11~0 t26~0 t3~0 t14~0 t18~0 t29~0(*1);

FS2 BY t4 t19 t7 t22 t15 t30 t5~0 t20~0
t9~0 t24~0 t12~0 t27~0 t1~0
t16~0 t2~0 t17~0 t8~0 t23~0 t13~0 t28~0
t6~0 t21~0 t10~0
t25~0 t11~0 t26~0 t3~0 t14~0 t18~0 t29~0(*1);

FS3 BY t1 t16 t2 t17 t8 t23 t13 t28 t4~0
t19~0 t7~0 t22~0 t15~0 t30~0 t5~0
t20~0 t9~0 t24~0 t12~0 t27~0 t6~0 t21~0
t10~0 t25~0 t11~0 t26~0 t3~0 t14~0 t18~0 t29~0(*1);

FS4 BY t6 t21 t10 t25 t11 t26 t5~0 t20~0
t9~0 t24~0 t12~0 t27~0 t4~0
t19~0 t7~0 t22~0 t15~0 t30~0 t1~0 t16~0
t2~0 t17~0 t8~0 t23~0 t13~0 t28~0
t3~0 t14~0 t18~0 t29~0(*1);

Some examples from Trait EI research

INPUT READING TERMINATED NORMALLY

Multiple Group Configural Invariance Gender Confi, Metric and Scalar.

SUMMARY OF ANALYSIS

Number of groups	2
Number of observations	
Group WOMAN	280
Group MAN	248
Total sample size	528
Number of dependent variables	30
Number of independent variables	0
Number of continuous latent variables	5

Observed dependent variables

Continuous

T1	T2	T3	T4	T5	T6
T7	T8	T9	T10	T11	T12
T13	T14	T15	T16	T17	T18
T19	T20	T21	T22	T23	T24
T25	T26	T27	T28	T29	T30

Continuous latent variables

EFA factors

*1:	FG	FS1	FS2	FS3	FS4
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Variables with special functions

Grouping variable GENDER

Estimator	MLR
Rotation	TARGET
Row standardization	Varies
Type of rotation	ORTHOGONAL
Information matrix	OBSERVED
Maximum number of iterations	1000
Convergence criterion	0.500D-04
Maximum number of steepest descent iterations	20
Optimization Specifications for the Exploratory Factor Analysis	
Rotation Algorithm	
Number of random starts	30
Maximum number of iterations	1000000
Derivative convergence criterion	0.100D-04

Input data file(s)
C:\full_new_dataset_clinical.dat

Input data format FREE

MODEL FIT INFORMATION FOR THE CONFIGURAL MODEL

Number of Free Parameters 400

Loglikelihood

H0 Value -29706.873
 H0 Scaling Correction Factor 1.3667
 for MLR
 H1 Value -29156.268
 H1 Scaling Correction Factor 1.1476
 for MLR

Information Criteria

Akaike (AIC) 60213.746
 Bayesian (BIC) 61921.385
 Sample-Size Adjusted BIC 60651.675
 (n* = (n + 2) / 24)

Chi-Square Test of Model Fit

Value 1102.298*
 Degrees of Freedom 590
 P-Value 0.0000
 Scaling Correction Factor 0.9990
 for MLR

Chi-Square Contribution and P-Value From Each Group (degrees of freedom = 295)

WOMAN 512.679 0.000
 MAN 589.618 0.000

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM and WLSMV cannot be used for chi-square difference testing in the regular way. MLM, MLR and WLSM chi-square difference testing is described on the Mplus website. MLMV, WLSMV, and ULSMV difference testing is done using the DIFFTEST option.

RMSEA (Root Mean Square Error Of Approximation)

Estimate 0.052
 90 Percent C.I. 0.052 0.063
 Probability RMSEA <= .05 0.011

CFI/TLI

CFI 0.885
 TLI 0.830

Chi-Square Test of Model Fit for the Baseline Model

Value 5311.345
 Degrees of Freedom 870
 P-Value 0.0000

SRMR (Standardized Root Mean Square Residual)

Value 0.039

MODEL FIT INFORMATION FOR THE METRIC MODEL

Number of Free Parameters 275

Loglikelihood

H0 Value -29827.804
 H0 Scaling Correction Factor 1.2673
 for MLR
 H1 Value -29156.268
 H1 Scaling Correction Factor 1.1476
 for MLR

Information Criteria

Akaike (AIC) 60205.609
 Bayesian (BIC) 61379.610
 Sample-Size Adjusted BIC 60506.685
 (n* = (n + 2) / 24)

Chi-Square Test of Model Fit

Value 1219.302*
 Degrees of Freedom 715
 P-Value 0.0000
 Scaling Correction Factor 1.1015
 for MLR

Chi-Square Contribution From Each Group

WOMAN 540.447
 MAN 678.856

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM and WLSMV cannot be used for chi-square difference testing in the regular way. MLM, MLR and WLSM chi-square difference testing is described on the Mplus website. MLMV, WLSMV, and ULSMV difference testing is done using the DIFFTEST option.

RMSEA (Root Mean Square Error Of Approximation)

Estimate 0.052
 90 Percent C.I. 0.047 0.057
 Probability RMSEA <= .05 0.283

CFI/TLI

CFI 0.886
 TLI 0.862

Chi-Square Test of Model Fit for the Baseline Model

Value 5311.345
 Degrees of Freedom 870
 P-Value 0.0000

SRMR (Standardized Root Mean Square Residual)

Value 0.052

MODEL FIT INFORMATION FOR THE SCALAR MODEL

Number of Free Parameters 275

Loglikelihood

H0 Value -29827.804
 H0 Scaling Correction Factor 1.2673
 for MLR
 H1 Value -29156.268
 H1 Scaling Correction Factor 1.1476
 for MLR

Information Criteria

Akaike (AIC) 60205.609
 Bayesian (BIC) 61379.610
 Sample-Size Adjusted BIC 60506.685
 (n* = (n + 2) / 24)

Chi-Square Test of Model Fit

Value 1219.302*
 Degrees of Freedom 715
 P-Value 0.0000
 Scaling Correction Factor 1.1015
 for MLR

Chi-Square Contribution From Each Group

WOMAN 540.447
 MAN 678.856

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM and WLSMV cannot be used for chi-square difference testing in the regular way. MLM, MLR and WLSM chi-square difference testing is described on the Mplus website. MLMV, WLSMV, and ULSMV difference testing is done using the DIFFTEST option.

RMSEA (Root Mean Square Error Of Approximation)

Estimate 0.052
 90 Percent C.I. 0.047 0.057
 Probability RMSEA <= .05 0.283

CFI/TLI

CFI 0.886
 TLI 0.862

Chi-Square Test of Model Fit for the Baseline Model

Value 5311.345
 Degrees of Freedom 870
 P-Value 0.0000

SRMR (Standardized Root Mean Square Residual)

Value 0.052

Some examples from Trait EI research

TITLE: Multiple Group **Configural Measurement Invariance** Across Genders

DATA:

FILE IS "C:\full_new_dataset_clinical.dat";

VARIABLE:

names= education occupation civilstatus age gender

t1 t2 t3 t4 t5 t6 t7 t8 t9 t10 t11 t12 t13 t14 t15 t16 t17 t18 t19 t20 t21 t22 t23 t24 t25 t26
t27 t28 t29 t30;

usevar = t1 t2 t3 t4 t5 t6 t7 t8 t9 t10 t11 t12 t13 t14 t15 t16 t17 t18 t19 t20 t21 t22 t23 t24
t25 t26 t27 t28 t29 t30;

grouping is gender (1=Woman 2=Man);

ANALYSIS:

ESTIMATOR = MLR;

ROTATION = TARGET (orthogonal);

MODEL:

fg BY t1-t30 (*1);

FS1 BY t5 t20 t9 t24 t12 t27 t4~0 t19~0 t7~0 t22~0 t15~0 t30~0 t1~0
t16~0 t2~0 t17~0 t8~0 t23~0 t13~0
t28~0 t6~0 t21~0 t10~0 t25~0 t11~0 t26~0 t3~0 t14~0 t18~0
t29~0(*1);

FS2 BY t4 t19 t7 t22 t15 t30 t5~0 t20~0 t9~0 t24~0 t12~0 t27~0 t1~0
t16~0 t2~0 t17~0 t8~0 t23~0 t13~0 t28~0 t6~0 t21~0 t10~0 t25~0
t11~0 t26~0 t3~0 t14~0 t18~0 t29~0(*1);

FS3 BY t1 t16 t2 t17 t8 t23 t13 t28 t4~0 t19~0 t7~0 t22~0 t15~0 t30~0
t5~0 t20~0 t9~0 t24~0 t12~0 t27~0 t6~0 t21~0 t10~0 t25~0 t11~0
t26~0 t3~0 t14~0 t18~0 t29~0(*1);

FS4 BY t6 t21 t10 t25 t11 t26 t5~0 t20~0 t9~0 t24~0 t12~0 t27~0 t4~0
t19~0 t7~0 t22~0 t15~0 t30~0 t1~0 t16~0 t2~0 t17~0 t8~0 t23~0
t13~0 t28~0 t3~0 t14~0 t18~0 t29~0(*1);

[t1-t30];

t1-t30;

[fg@0]; [FS1@0]; [FS2@0]; [FS3@0]; [FS4@0];

OUTPUT:

sampstat standardized SVALUES stdyx modindices(15);

MODEL Man:

fg BY t1-t30 (*1);
FS1 BY t5 t20 t9 t24 t12 t27 t4~0 t19~0
t7~0 t22~0 t15~0 t30~0 t1~0
t16~0 t2~0 t17~0 t8~0 t23~0 t13~0
t28~0 t6~0 t21~0 t10~0
t25~0 t11~0 t26~0 t3~0 t14~0 t18~0 t29~0(*1);
FS2 BY t4 t19 t7 t22 t15 t30 t5~0 t20~0
t9~0 t24~0 t12~0 t27~0 t1~0
t16~0 t2~0 t17~0 t8~0 t23~0 t13~0 t28~0
t6~0 t21~0 t10~0
t25~0 t11~0 t26~0 t3~0 t14~0 t18~0 t29~0(*1);
FS3 BY t1 t16 t2 t17 t8 t23 t13 t28 t4~0
t19~0 t7~0 t22~0 t15~0 t30~0 t5~0
t20~0 t9~0 t24~0 t12~0 t27~0 t6~0 t21~0
t10~0 t25~0 t11~0 t26~0 t3~0 t14~0 t18~0 t29~0(*1);
FS4 BY t6 t21 t10 t25 t11 t26 t5~0 t20~0
t9~0 t24~0 t12~0 t27~0 t4~0
t19~0 t7~0 t22~0 t15~0 t30~0 t1~0 t16~0
t2~0 t17~0 t8~0 t23~0 t13~0 t28~0
t3~0 t14~0 t18~0 t29~0(*1);

Configural Measurement Invariance

THE MODEL ESTIMATION TERMINATED NORMALLY

MODEL FIT INFORMATION

Number of Free Parameters 275

Loglikelihood

H0 Value	-29827.804
H0 Scaling Correction Factor for MLR	1.2673
H1 Value	-29156.268
H1 Scaling Correction Factor for MLR	1.1476

Information Criteria

Akaike (AIC)	60205.609
Bayesian (BIC)	61379.610
Sample-Size Adjusted BIC ($n^* = (n + 2) / 24$)	60506.685

Chi-Square Test of Model Fit

Value	1219.302*
Degrees of Freedom	715
P-Value	0.0000
Scaling Correction Factor for MLR	1.1015

Chi-Square Contribution From Each Group

WOMAN	540.447
MAN	678.856

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM and WLSMV cannot be used for chi-square difference testing in the regular way. MLM, MLR and WLSM chi-square difference testing is described on the Mplus website. MLMV, WLSMV, and ULSMV difference testing is done using the DIFFTEST option.

RMSEA (Root Mean Square Error Of Approximation)

Estimate	0.052
90 Percent C.I.	0.047 0.057
Probability RMSEA <= .05	0.283

CFI/TLI

CFI	0.886
TLI	0.862

Chi-Square Test of Model Fit for the Baseline Model

Value	5311.345
Degrees of Freedom	870
P-Value	0.0000

SRMR (Standardized Root Mean Square Residual)

Value	0.052
-------	-------

Some examples from Trait EI research

TITLE: Multiple Group Metric Measurement Invariance Across Genders

[t1-t30]; ← Item intercepts

t1-t30; ← Item uniqueness

[fg@0]; [FS1@0]; [FS2@0]; [FS3@0]; [FS4@0]; ← Factor means

Factor loadings are freed here so no need to include “Model Man” anymore

T18 WITH T3;
T19 WITH T4;
T24 WITH T9;
T30 WITH T7;
T17 WITH T2;
T25 WITH T10;

Correlated uniquenesses

Metric Measurement Invariance

THE MODEL ESTIMATION TERMINATED NORMALLY

MODEL FIT INFORMATION

Number of Free Parameters 245

Loglikelihood

H0 Value -29854.004
H0 Scaling Correction Factor for MLR 1.3127
H1 Value -29156.268
H1 Scaling Correction Factor for MLR 1.1476

Information Criteria

Akaike (AIC) 60198.007
Bayesian (BIC) 61243.936
Sample-Size Adjusted BIC 60466.239
(n* = (n + 2) / 24)

Chi-Square Test of Model Fit

Value 1276.417*
Degrees of Freedom 745
P-Value 0.0000
Scaling Correction Factor for MLR 1.0933

Chi-Square Contribution From Each Group

WOMAN	566.828
MAN	709.589

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM and WLSMV cannot be used for chi-square difference testing in the regular way. MLM, MLR and WLSM chi-square difference testing is described on the Mplus website. MLMV, WLSMV, and ULSMV difference testing is done using the DIFFTEST option.

RMSEA (Root Mean Square Error Of Approximation)

Estimate	0.052
90 Percent C.I.	0.047 0.057
Probability RMSEA <= .05	0.247

CFI/TLI

CFI	0.880
TLI	0.860

Chi-Square Test of Model Fit for the Baseline Model

Value	5311.345
Degrees of Freedom	870
P-Value	0.0000

SRMR (Standardized Root Mean Square Residual)

Value	0.054
-------	-------

MODEL MODIFICATION INDICES

NOTE: Modification indices for direct effects of observed dependent variables regressed on covariates may not be included. To include these, request MODINDICES (ALL).

Minimum M.I. value for printing the modification index 15.000

Group	M.I.	E.P.C.	Std E.P.C.	StdYX E.P.C.
Group WOMAN				

WITH Statements

T18	WITH T3	29.896	0.723	0.723	0.375
T19	WITH T4	19.887	0.709	0.709	0.296
T24	WITH T9	17.806	0.477	0.477	0.397
T28	WITH T6	29.682	0.822	0.822	0.382
T30	WITH T7	16.293	0.810	0.810	0.265

Group MAN

WITH Statements

T11	WITH T9	15.109	0.430	0.430	0.390
T17	WITH T2	17.364	0.712	0.712	0.296
T25	WITH T10	18.598	0.934	0.934	0.302

Some examples from Trait EI research

TITLE: Multiple Group Scalar Measurement Invariance Across Genders

[t1-t30]; ← Item intercepts are now invariant across groups

t1-t30; ← Item uniqueness (residuals)

[fg@0]; [FS1@0]; [FS2@0]; [FS3@0]; [FS4@0];

← Factor means were set to be equal

[fg*]; [FS1*]; [FS2*]; [FS3*]; [FS4*];

← Factor means set to be freely estimated across groups



Scalar Measurement Invariance

MODEL FIT INFORMATION

Number of Free Parameters	250
Loglikelihood	
H0 Value	-29845.373
H0 Scaling Correction Factor for MLR	1.4101
H1 Value	-29156.268
H1 Scaling Correction Factor for MLR	1.1476
Information Criteria	
Akaike (AIC)	60190.747
Bayesian (BIC)	61258.021
Sample-Size Adjusted BIC (n* = (n + 2) / 24)	60464.453
Chi-Square Test of Model Fit	
Value	1301.574*
Degrees of Freedom	740
P-Value	0.0000
Scaling Correction Factor for MLR	1.0589

Chi-Square Contribution From Each Group

WOMAN	578.240
MEN	723.334

* The chi-square value for MLM, MLMV, MLR, ULSMV, WLSM and WL for chi-square difference testing in the regular way. MLM, chi-square difference testing is described on the Mplus web and ULSMV difference testing is done using the DIFFTEST opt

RMSEA (Root Mean Square Error Of Approximation)

Estimate	0.054
90 Percent C.I.	0.049 0.058
Probability RMSEA <= .05	0.107

CFI/TLI

CFI	0.874
TLI	0.851

Chi-Square Test of Model Fit for the Baseline Model

Value	5311.345
Degrees of Freedom	870
P-Value	0.0000

SRMR (Standardized Root Mean Square Residual)

Value	0.053
-------	-------

MODEL MODIFICATION INDICES

NOTE: Modification indices for direct effects of observed dependent variables regressed on covariates may not be included. To include these, request MODINDICES (ALL).

Minimum M.I. value for printing the modification index 15.000

	M.I.	E.P.C.	Std E.P.C.	StdYX E.P.C.
Group WOMAN				

WITH Statements

T18	WITH T3	30.985	0.724	0.724	0.375
T19	WITH T4	19.749	0.694	0.694	0.293
T24	WITH T9	18.840	0.479	0.479	0.398
T28	WITH T6	29.846	0.809	0.809	0.381
T30	WITH T7	16.704	0.807	0.807	0.264

Group MEN

WITH Statements

T11	WITH T9	15.583	0.429	0.429	0.374
T17	WITH T2	18.177	0.715	0.715	0.299
T25	WITH T10	18.983	0.928	0.928	0.300

Some examples from Trait EI research

TITLE: Multiple Group Strict Measurement Invariance Across Genders

t1-t30; ← Item uniqueness (residuals) are now invariant across groups

[fg*]; [FS1*]; [FS2*]; [FS3*]; [FS4*];

Factor means are freely estimated across groups, as when testing scalar invariance.

Reporting of Measurement Invariance

Pérez-Díaz & Petrides, 2021

Table 4. Multiple group measurement invariance model comparisons.

Models	χ^2	$\Delta \chi^2$	df	CFI	ΔCFI	RMSEA	$\Delta RMSEA$	RMSEALb	RMSEAUb	SRMR	$\Delta SRMR$
1											
Configural	1506.16	—	879	0.917	—	0.046	—	0.042	0.050	0.036	—
Metric	2031.69	525.53	1129	0.880	0.037	0.049	0.003	0.046	0.053	0.054	0.018
Scalar	2253.93	222.24	1179	0.857	0.023	0.053	0.004	0.049	0.056	0.061	0.007
2											
Configural	1121.93	—	586	0.927	—	0.043	—	0.039	0.047	0.032	—
Metric	1398.02	276.09	711	0.907	0.020	0.044	0.001	0.041	0.048	0.044	0.012
Scalar	1593.17	195.15	736	0.884	0.023	0.048	0.004	0.045	0.052	0.049	0.005
3											
Configural	783.80	—	584	0.946	—	0.039	—	0.031	0.046	0.037	—
Metric	1013.49	229.69	709	0.918	0.028	0.043	0.004	0.037	0.049	0.052	0.015
Scalar	1053.43	39.94	734	0.914	0.004	0.044	0.001	0.038	0.050	0.055	0.003
4											
Configural	1135.40	—	588	0.916	—	0.046	—	0.042	0.050	0.034	—
Metric	1414.86	279.46	713	0.892	0.024	0.048	0.002	0.044	0.051	0.047	0.013
Scalar	1576.47	161.61	738	0.871	0.021	0.051	0.003	0.048	0.055	0.053	0.006

Note. Model 1 = UK validation sample, N = 537; Chilean general population, N = 335; and Chilean clinical population, N = 120. Model 2 = UK validation sample and combined Chilean samples. Model 3 = Chilean general and clinical samples. Model 4 = UK validation sample and Chilean general population. χ^2 = Chi Squared, $\Delta \chi^2$ = Chi Square difference, df = degrees of freedom, CFI = Comparative Fit Index, ΔCFI = CFI difference, RMSEA = Root Mean Square Error of Approximation, $\Delta RMSEA$ = RMSEA difference, RMSEALb = RMSEA Lower bound, RMSEAUb = Upper bound. SRMR = Standardized root mean residual, $\Delta SRMR$ = SRMR difference.

Reporting of Measurement Invariance

Pérez-Díaz et al., 2021


TABLE 1 | Multiple group measurement invariance comparisons by sociodemographic characteristics.

Models	χ^2	$\Delta \chi^2$	df	CFI	ΔCFI	RMSEA	$\Delta RMSEA$	RMSEALb	RMSEAUb	SRMR	$\Delta SRMR$
1. Gender											
Configural	1070.90	–	703	0.917	–	0.045	–	0.039	0.050	0.049	–
Metric	1120.81	49.91	733	0.913	0.004	0.045	0.000	0.039	0.050	0.052	0.003
Scalar	1099.95	20.86	728	0.916	0.003	0.044	0.001	0.039	0.049	0.051	0.001
2. Age											
Configural	1085.76	–	586	0.887	–	0.057	–	0.052	0.062	0.040	–
Metric	1164.16	78.40	737	0.904	0.017	0.047	0.010	0.042	0.052	0.051	0.011
Scalar	1323.80	159.64	732	0.866	0.028	0.055	0.008	0.051	0.060	0.051	0.000
3. Education											
Configural	1576.51	–	1114	0.901	–	0.049	–	0.043	0.054	0.061	–
Metric	1664.21	87.70	1174	0.896	0.005	0.049	0.000	0.043	0.054	0.065	0.004
Scalar	1646.01	18.20	1164	0.897	0.001	0.049	0.000	0.043	0.054	0.062	0.003
4. Civil status											
Configural	1642.57	–	1117	0.884	–	0.054	–	0.049	0.060	0.063	–
Metric	1861.72	122.09	1192	0.894	0.010	0.051	0.001	0.047	0.056	0.067	0.012
Scalar	1755.58	106.14	1180	0.873	0.019	0.055	0.004	0.050	0.061	0.069	0.002
5. Occupation											
Configural	1713.73	–	1123	0.861	–	0.060	–	0.054	0.066	0.067	–
Metric	1798.55	84.82	1183	0.855	0.006	0.060	0.000	0.054	0.065	0.072	0.005
Scalar	1792.44	6.11	1173	0.854	0.001	0.060	0.000	0.055	0.066	0.069	0.003





Model 1 = gender, $N = 528$, $nWomen = 280$, $nMen = 248$. Model 2 = age, $N = 528$, $nYoung = 230$, $nSenior = 298$. Model 3 = education, $N = 528$, $nSecondary = 187$, $nUniversity = 257$, $nGraduate = 84$. Model 4 = civil status, $N = 479$, $nSingle = 273$, $nRelationship = 118$, $nMarried = 88$. Model 5 = occupation, $N = 438$, $nPrivate = 164$, $nPublic = 114$, $nStudent = 160$. χ^2 = chi squared, $\Delta \chi^2$ = chi squared difference, df = degrees of freedom, CFI = comparative fit index, ΔCFI = CFI difference, $RMSEA$ = root mean square error of approximation, $\Delta RMSEA$ = $RMSEA$ difference, $RMSEALb$ = $RMSEA$ lower bound, $RMSEAUb$ = $RMSEA$ upper bound. $SRMR$ = standardised root mean residual, $\Delta SRMR$ = $SRMR$ difference.

Suggested resources

Go to the supplementary material!

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An Illustration of the Exploratory Structural Equation Modeling (ESEM) Framework on the Passion Scale

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While exploratory factor analysis (EFA) provides a more realistic presentation of the data with the allowance of item cross-loadings, confirmatory factor analysis (CFA) includes many methodological advances that the former does not. To create a synergy of the two, exploratory structural equation modeling (ESEM) was proposed as an alternative solution, incorporating the

Articles

The Spanish-Chilean Trait Emotional Intelligence Questionnaire-Short Form: The Adaptation and Validation of the TEIQue-SF in Chile

Pablo A. Pérez-Díaz  & K. V. Petrides 

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